



Research Article

**BAYESIAN NETWORK MODEL OF TURKISH FINANCIAL MARKET FROM YEAR-TO-SEPTEMBER 30<sup>TH</sup> OF 2016**

**Ersin SENER<sup>1</sup>, Hasan Aykut KARABOGA\*<sup>2</sup>, Ibrahim DEMIR<sup>3</sup>**

<sup>1</sup>*Dept. of Mathematics, Kırklareli University, KIRKLARELI; ORCID: 0000-0002-5934-3652*

<sup>2</sup>*Department of Statistics, Yildiz Technical University, Esenler-ISTANBUL; ORCID: 0000-0001-8877-3267*

<sup>3</sup>*Department of Statistics, Yildiz Technical University, Esenler-ISTANBUL; ORCID: 0000-0002-2734-4116*

**Received: 16.09.2019 Accepted: 11.11.2019**

**ABSTRACT**

Bayesian Networks (BNs) are a useful graphical probabilistic structure for visualizing and understanding the dependencies of random variables. In this study, July 15 coup attempts' effects on Turkish Financial Market are analyzed with the BN approach. To this end, 31 Istanbul Stock Exchange (BIST) return indexes and seven foreign exchange rates (CNY, EUR, GBP, JPY, SAR, RUB, and USD) from year-to-September 30<sup>th</sup> of 2016 are examined. BN structure is learned (predicted) via Greedy Thick Thinning algorithm with K2 prior from the dataset and is expertized. BN model is validated and trained from real dataset instead of generated data from the established model. The BN is called Trained Bayesian Network (TBN) model. TBN is validated and the beliefs of TBN are updated again by dataset via learning parameters with Expectation Maximization (EM) algorithm. BNs have not before been used to relate the presence/absence of BIST return indexes with foreign exchange rates. Accuracy rate (AUC) of the TBN model to generating the real data is calculated as 85.5% percent. TBN model has simplified the Market relations with conditional probability.

**Keywords:** Bayesian network, structure learning, Istanbul stock exchange return indexes, foreign exchange rate, Receiver Operating Characteristic (ROC).

**1. INTRODUCTION**

Bayesian Networks (BNs) are very popular and mostly used for understanding complex conditional relation structures. These techniques suggest a mathematical model for representing uncertain information with accruing probabilities of variables by Directed Acyclic Graph (DAG) structures [1, 2]. The structure of model is reflected by the graphical part of BNs, while local interactions among correlated variables are calculating via conditional probability distributions. These features make the BNs attractive for all decision-making and modelling areas.

In financial analysis, BNs are being used for bankruptcy or failure prediction [3-5], credit risk modelling or credit scoring [6-8], portfolio risk analysis [9], firm performance evaluation [10], company appraising [11], supply chain analysis [12] etc. on the business and finance area up to the present. BNs have ascending popularity especially, in the risk management and assessment area [13].

\* Corresponding Author: e-mail: karaboga@yildiz.edu.tr, tel: (212) 383 44 27

As it is clear from the literature, researchers use BNs for financial risk assessment to evaluate an organization. BN model established in estimating stock prices for determination, validation and forecasting, respectively is a better predictor than AR, MA, ARMA and ARCH models [14]. For credit rating, different MCMC BN classifiers from the three real-life datasets are compared and performed very well with the support of the Markov Blanket concept [15]. The Czech engineering sector and its sub-sectors have been investigated by BN model established with expert knowledge and data on 4400 financial reports obtained between 1993 and 1997 [16]. BN is compared with neural network on financial rating analysis [17]. Ant Colony Optimized BN model is applied with two different algorithms (ChainACO and K2ACO) to find the factors that affect the rural property mortgages. ChainACO is cheaper than K2ACO, but K2ACO has better BN structure [18]. The results of the BN model developed for estimating the Up/down analysis of Nikkei, Dow30 and FSTE100 are compared with the psychological line and trend prediction analysis and the BN algorithm is given a higher profit than the conventional analysis [19]. In the studies with the credit rating system related to the BN evaluation model, the cause and effect relationship of the BN was used in developing a risk analysis tool for bank credits and the dynamic model is criticized for adaptation into new situation or environment by adding a node [20]. A review of BN references about maintenance applications, dependability of variables and risk analysis is presented and dependability analyses methods namely Fault Trees (FT), Markov Chains (MC) and Petri Nets (PN) are discussed [21]. BNs are used to improve risk profiles of contractors [13]. BN model is presented to analyze portfolio returns with basic economic variables from Polish financial market [22]. One of the studies takes advantage of BN using financial indexes to show the dissimilarities between different industries [23]. BN is used to turn an account for customer satisfaction [24]. BN models are proposed to demonstrate the practicability of financial risks' Bayesian modelling on e-logistics investments [25].

The aim of us is to predict the relation between the 31 return indexes of BIST and 7 foreign exchange by using BN. Three subheadings of BNs as structure learning, parameter learning and model validation, respectively have also been studied via GeNIe, which is general purpose-development environment for graphical decision-analytic models [26]. In the structure learning; Greedy Thick Thinning algorithm, which is heuristic search algorithm, with K2 prior has been used for structure learning of BN from the *training-dataset*. The BN is finalized after expert opinion by revising the direction of the arc between the nodes with taking into account the relations. In the parameter learning, parameter of model is learnt with EM algorithm and beliefs of BN are updated via the *validation-dataset*. And then, BN Model is validated on *test-dataset* via 10-fold cross-validation with zero seed. The model has been successfully obtained and tested. Consequently, The BN is interpreted with 12 different scenarios for decreasing, increasing and recession positions of indexes and foreign exchange rates. Four scenarios are queried from the TBN model.

## 2. MATERIALS AND METHOD

In this section, we mention examined datasets and methods, which is used for analysis.

### 2.1. Materials

In the present study, we examined 31 return indexes of BIST and 7 foreign exchange rates year-to-Sept 30, 2016. Data, which is presented in Appendix Table A.1, is collected from borsaistanbul.com and tcmb.gov.tr by the end of workday and organized with regard to the ratio of percentage change of BIST return indexes and foreign exchange rates. Since indexes are continuous variables and generally have a normal distribution. Those ratios are also continuous but are categorized to construct BN model. However, some methods are available discretizing the indexes [22]. Thus, the ratios are binned into intervals as decreasing (< -.05 percent), increasing

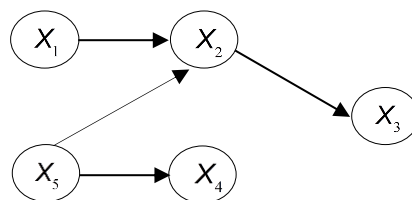
(> .05 percent) and recession ( $-.05 < <.05$ ). Afterward s, data was separated into three terms for analysis. *1<sup>st</sup> term data (training-dataset; January-April, 30<sup>th</sup>)* is used for constructing BN structure via Greedy Thick Thinning (GTT), which is a heuristic search method with K2 prior. *2<sup>nd</sup> term data (validation-dataset; May-July, 15<sup>th</sup>)* is used for training BN via learning parameters with EM algorithm and updating beliefs of BN. *3<sup>rd</sup> term data (test-dataset; July, 18<sup>th</sup>-September, 30<sup>th</sup>)* is used for validating TBN via 10-crossvalidation with zero seed and updating beliefs of TBN.

**2.2. Method**

The methods used in the study and the requirements for the use of these methods will be discussed in this section.

**2.3. Bayesian Network**

BNs are effective tools for modelling complex problems involving uncertain information [27]. Best of the inspiring characteristics of the BN's is evidence propagation. The mentioned characteristic allows updating probabilities of each node bi-directionally from one node through whole structure with a new knowledge [28]. BNs are used to construct mathematical models by taking advantage of the conditional probability values to determine the interaction and relationship between variables. BNs contain two main information; one of DAG for determining the relation of variables and the other is mathematical equations to make inference on parameters of the model. Features of graph and probability theory are combined [29, 30]. A DAG is a mathematical object defined as the pair  $G = (B, C)$ , where  $B$  is the set of nodes (variables) and  $C$  is the set of directed edges (arcs) connecting pair of nodes. An example of DAG is shown in Fig. 1. Arc represent dependencies between nodes(variables).



**Figure 1.** An Example of DAG

BN is given for  $K$  variables ( $i = 1, \dots, K, K \in B$ ). Each node  $X$  is associated with the conditional probability distribution of the corresponding variable of interest given its parents,  $p(X / pa(X_i))$ . We can represent the joint probability distribution of  $(X_1, \dots, X_K)$  according to DAG is represented Eq. (1).

$$p(X_1, \dots, X_K) = \prod_{i \in B} p(X_i / pa(X_i)) \tag{1}$$

Mathematical model of Fig. 1 is presented Eq. (2).

$$p(X_1, X_2, X_3, X_4, X_5) = p(X_1) p(X_3 / X_2) p(X_2 / X_1, X_5) p(X_4 / X_5) p(X_5) \tag{2}$$

The BN can generally be dealt with under three main headings: structure learning, parameter learning and model validation. Structure learning algorithms are categorized in two groups as score-based algorithms and constraint-based algorithms [2, 31]. At the base of score-based search

algorithms is to assign a score to each possible BN and specify the network that maximizes this score by heuristic search algorithms. On the other hand, constraint-based algorithms learn the network structure by using the Markov properties of BNs together with conditional independence tests and examining the probabilistic relationship between variables. After that, network graph structure is constructed as a BN. Constraint-based structure learning algorithms are originally based on Inductive Causation (IC) algorithm [32]. Constraint-based structure learning methods with heuristic search algorithms are generally used to analyze BNs with relations between the variables as DAG structures. Although there is many search procedures in the literature, the greedy search algorithm is generally used as it is in this study.

#### **2.4. Greedy Thick Thinning**

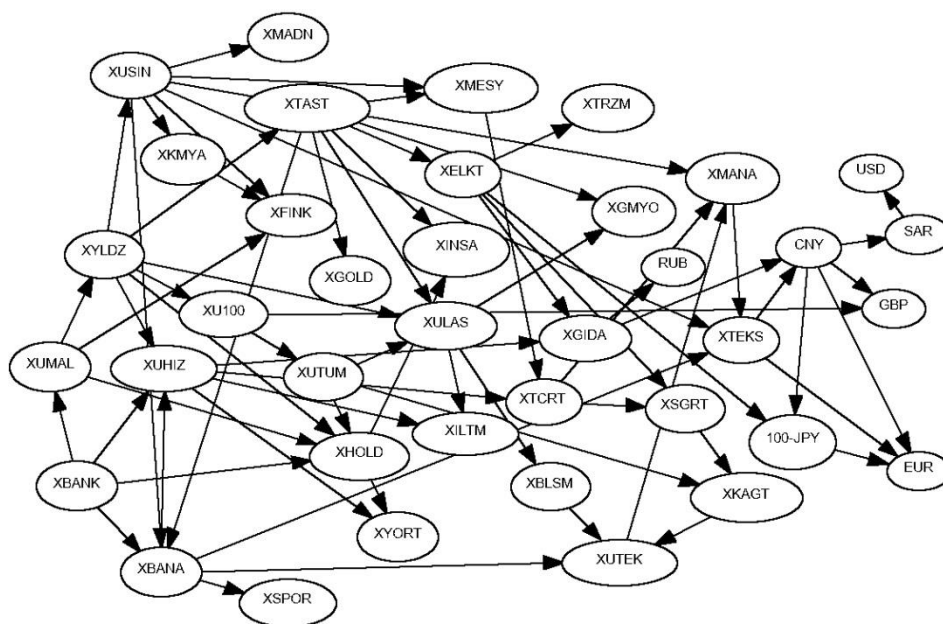
In many studies on structure learning of BNs have been discussed the GTT algorithm with K2 prior [31, 33, 34] is more successful than the other Greedy Search algorithms [1, 24, 35-37].

Greedy search is one of the methods for escaping local maxima with random restarts and known as a useful simple heuristic search approximation algorithm [38, 39]. GTT, a constraint-based heuristic search algorithm for BN structure learning, is based on the Bayesian search approach [35]. Firstly, The GTT algorithm creates a null graph based on the probabilities of the variables (nodes) and their conditional probabilities. GTT then adds an edge between the nodes if there is no conditional independence between the nodes. Finally, because of repetitive checks, the edges of the connected nodes that are independent on the graph are subtracted if any. In short, the GTT algorithm is a topology optimizer that exploits variables and dependency relations.

If there is sufficient information about the sub-factors and interaction of the study, the BNs' DAG model can be manually constructed within the framework of the expert opinion. Although we have enough knowledge about the variables of our model, it is necessary to learn (predict) the model from the existing data in the construction of the DAG model of the complex structure about financial data. The final decision of the model's DAG structure with the expert opinion is important in that the analysis produces meaningful results.

### **3. RESULTS**

One of the heuristic search algorithms known constraint-based structure learning method Greedy Thick Thinning algorithm with K2 prior used for constructing BN Model via GeNIe 2.2 Academic Edition.



**Figure 2.** Trained BN(TBN) structure (Main Model) of return indexes and exchange rate

The BN structure of 31 return indexes and 7 exchange rates have calculated based on the 1st term data, using the GTT algorithm with K2 prior (see Fig. 2). BN is established by using the expert opinion to determine the dependency relations (parent/child) between the nodes.

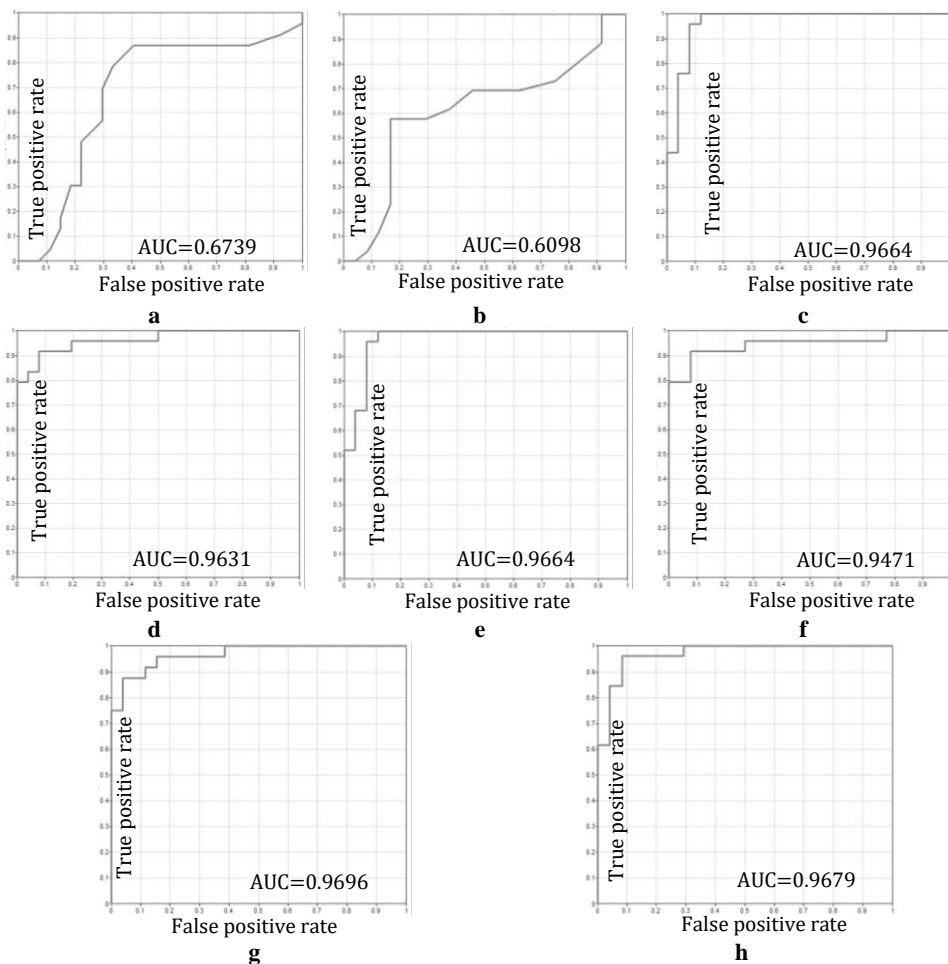
BN model parameters are learnt (predict) from 2nd term data with  $\log(p) = -998.574309$  via Expectation Maximization (EM) algorithm. BNs make it easy to see the model dynamically. After learning the parameters of BN model, The BN is validated via 10-fold cross-validation method with zero seed. In the new data stream of the model variables, the networks can be updated and new output can be generated by focusing only on the affected areas of the network. BNs can be transparent and supervised. Then, beliefs of BN main model are updated from the 2<sup>nd</sup> term data and BN is called Trained Bayesian Network (TBN) Model.

In the performance analysis of the model where multiple nodes are targeted, the cross-validation scheme is quite successful [40]. TBN model is tested and is performed from 3<sup>rd</sup> term data. XGMYO, XU100, XUTUM, XYLDZ indexes, which are the most effected variables on the TBN, are compared using the Receiver Operating Characteristic (ROC) curve, which is expressed as the ratio of true positives to false positives [41], the Area under the ROC (AUC) are shown in Fig. 3. Then, beliefs of TBN model are updated from the 3<sup>rd</sup> term data.

AUC rates values, which are ranges between 0 and 1, are shown that how well the TBN model can distinguish between of BIST return indexes to foreign exchange rates (absence/presence) in Table 1.

Accuracy rate of the TBN model to generating the real data (*test-dataset*) is calculated as 85.5%. Note that this result is obtained for the overall accuracy rate with absence and presence accuracy rates. Usages of real data ensure that the TBN model is re-trained. Thus, it was possible to calculate the conditional probabilities in different situations in this model.

Three different return indexes (XUTUM, XUHIZ, XBANK) and one foreign exchange rate were examined for three different conditions (decreasing, recession, increasing), separately and 12 different scenarios are tested in Table 2.



**Figure 3.** Receiver Operating Characteristic (ROC) curves and Area Under the ROC (AUC) for TBN model of us generated by Greedy Thick Thinning algorithm with K2 prior are shown; (a) ROC curve for decreasing condition of XGMYO, (b) ROC curve for increasing condition of XGMYO, (c) ROC curve for decreasing condition of XU100, (d) ROC curve for increasing condition of XU100, (e) ROC curve for decreasing condition of XUTUM, (f) ROC curve for increasing condition of XUTUM, (g) ROC curve for decreasing condition of XYLDZ, (h) ROC curve for increasing condition of XYLDZ.

**Table 1.** Accuracy rates (in percentage) of four indexes for BN model

| Indexes | Accuracy | Absence <sup>1</sup> | Presence <sup>2</sup> |
|---------|----------|----------------------|-----------------------|
| XGMYO   | 70.0     | 57.7                 | 87.0                  |
| XU100   | 92.0     | 91.67                | 96.0                  |
| XUTUM   | 90.0     | 91.67                | 92.0                  |
| XYLDZ   | 90.0     | 87.5                 | 92.3                  |

1. Accuracy rate for index value decreasing.

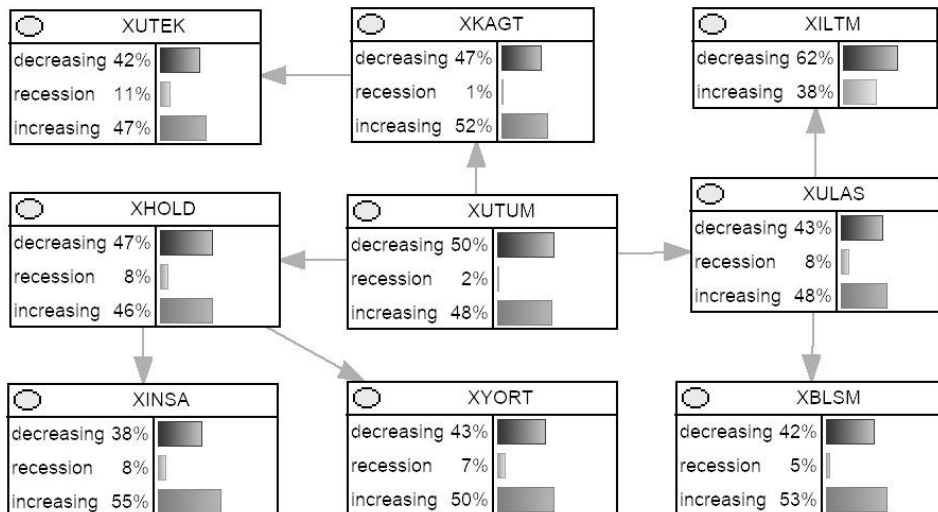
2. Accuracy rate for index value increasing.

**Table 2.** Evidential Scenarios About Some Important Variables

|              | SCENERIOS   |       |       |              |      |      |               |      |      |              |      |      |
|--------------|-------------|-------|-------|--------------|------|------|---------------|------|------|--------------|------|------|
|              | I. Scenario |       |       | II. Scenario |      |      | III. Scenario |      |      | IV. Scenario |      |      |
|              | 1           | 2     | 3     | 4            | 5    | 6    | 7             | 8    | 9    | 10           | 11   | 12   |
| <b>XUTUM</b> |             |       |       |              |      |      |               |      |      |              |      |      |
| Decreasing   | 100         |       |       | 72.5         | 58.4 | 19.8 | 86.2          | 72   | 11.5 | 51.4         | 46   | 48.9 |
| Recession    |             | 100   |       | 3            | 3    | 1    | 3.4           | 2.9  | .9   | 2.2          | 2    | 2.2  |
| Increasing   |             |       | 100   | 24.5         | 38.7 | 79.2 | 10.5          | 25.1 | 87.6 | 46.4         | 52   | 48.9 |
| <b>XU100</b> |             |       |       |              |      |      |               |      |      |              |      |      |
| Decreasing   | 99.98       | .10   | .04   | 72.5         | 58.3 | 19.7 | 86.1          | 71.9 | 11.4 | 51.4         | 46   | 48.9 |
| Recession    | .01         | 99.75 | .01   | 3.1          | 3    | 1    | 3.4           | 3    | .9   | 2.3          | 2    | 2.2  |
| Increasing   | .01         | .15   | 99.95 | 24.4         | 38.6 | 79.3 | 10.4          | 25.1 | 87.6 | 46.4         | 52   | 48.9 |
| <b>XYLDZ</b> |             |       |       |              |      |      |               |      |      |              |      |      |
| Decreasing   | 99.96       | 86.1  | .01   | 75.3         | 60.5 | 20.5 | 89.5          | 74.7 | 11.9 | 53.3         | 47.7 | 50.8 |
| Recession    | .03         | 13.6  | .02   | .4           | 1.1  | .3   | .2            | .3   | .6   | .4           | .4   | .4   |
| Increasing   | .01         | .3    | 99.7  | 24.4         | 38.4 | 79.2 | 10.3          | 25   | 87.5 | 46.3         | 51.9 | 48.8 |
| <b>XUHIZ</b> |             |       |       |              |      |      |               |      |      |              |      |      |
| Decreasing   | 74.5        | 70.7  | 26    | 100          |      |      | 79            | 24.2 | 25.3 | 52           | 47.1 | 51   |
| Recession    | 9.2         | 10.8  | 6.3   |              | 100  |      | 7.4           | 24.2 | 7    | 7.6          | 6.5  | 8.3  |
| Increasing   | 16.3        | 18.5  | 67.7  |              |      | 100  | 13.6          | 51.6 | 67.7 | 40.4         | 46.4 | 40.6 |
| <b>XGMYO</b> |             |       |       |              |      |      |               |      |      |              |      |      |
| Decreasing   | 62.2        | 46.2  | 26.9  | 53.8         | 47.7 | 33.2 | 58            | 52.9 | 31.1 | 45.5         | 43.1 | 44.7 |
| Recession    | 2           | 4.1   | 4.5   | 2.3          | 3.2  | 4.4  | 2.3           | 2.7  | 4.2  | 3.2          | 3.4  | 3.2  |
| Increasing   | 35.8        | 49.7  | 68.6  | 43.9         | 49.1 | 62.4 | 39.7          | 44.4 | 64.7 | 51.3         | 53.4 | 52.1 |
| <b>XGIDA</b> |             |       |       |              |      |      |               |      |      |              |      |      |
| Decreasing   | 58          | 57.2  | 42.4  | 57.4         | 69.6 | 38.2 | 57.4          | 54.7 | 43.2 | 48.3         | 33   | 56.2 |
| Recession    | 7.7         | 7.6   | 3.7   | 9            | 11.7 | .6   | 7.9           | 5.3  | 3.7  | 5.6          | 4.8  | 6.1  |
| Increasing   | 34.3        | 35.2  | 53.9  | 33.6         | 18.7 | 61.2 | 34.7          | 40   | 53.2 | 46.1         | 62.2 | 37.7 |
| <b>XBANK</b> |             |       |       |              |      |      |               |      |      |              |      |      |
| Decreasing   | 83.3        | 74.5  | 10.5  | 74.3         | 45.1 | 15.9 | 100           |      |      | 49.7         | 44.5 | 47.2 |
| Recession    | 5.7         | 5.3   | 2     | 1.9          | 12.1 | 4.9  |               | 100  |      | 4            | 3.8  | 3.9  |
| Increasing   | 11.1        | 20.3  | 87.5  | 23.8         | 42.8 | 79.2 |               |      | 100  | 46.3         | 51.7 | 48.9 |
| <b>XHOLD</b> |             |       |       |              |      |      |               |      |      |              |      |      |
| Decreasing   | 82.3        | 24.1  | 10.6  | 63.9         | 51.1 | 24.1 | 75.2          | 62.9 | 16.6 | 47.8         | 43.8 | 45.9 |
| Recession    | 10.1        | 56.8  | 3     | 10.7         | 11.9 | 3.8  | 12.1          | 20.4 | 2.1  | 7.8          | 7.2  | 7.6  |
| Increasing   | 7.7         | 19.1  | 86.4  | 25.9         | 37   | 72.1 | 12.7          | 16.6 | 81.3 | 44.4         | 49   | 46.4 |
| <b>XGOLD</b> |             |       |       |              |      |      |               |      |      |              |      |      |
| Decreasing   | 51.2        | 51.4  | 52.8  | 52.1         | 51.6 | 51.9 | 51.4          | 51.6 | 52.6 | 51.9         | 52   | 52   |
| Recession    | 2.3         | 2.4   | 3.4   | 2.3          | 2.8  | 3.5  | 2.4           | 2.6  | 3.3  | 2.8          | 3    | 2.8  |
| Increasing   | 46.5        | 46.2  | 43.8  | 45.6         | 45.7 | 44.6 | 46.2          | 45.8 | 44.1 | 45.2         | 45   | 45.2 |
| <b>USD</b>   |             |       |       |              |      |      |               |      |      |              |      |      |
| Decreasing   | 45.3        | 44.9  | 42.3  | 44.7         | 42.5 | 43.1 | 45.4          | 44.4 | 42.3 | 100          |      |      |
| Recession    | 9           | 9.1   | 10.6  | 9            | 8.1  | 11   | 9             | 9.5  | 10.5 |              | 100  |      |
| Increasing   | 45.7        | 46    | 47.2  | 46.3         | 49.4 | 45.9 | 45.6          | 46.1 | 47.2 |              |      | 100  |

Some evidential scenarios have given in Table 2. Each scenario gives a percentage of 100% for one case. All cases are especially conditional probabilities. This means that, for example if we know XUTUM will decrease, XU100's decreasing probability will be 99.98%. On the other hand, posterior probabilities of recession and increasing are .01%.

**Note that,** the probability values of indexes and foreign exchange rate, which are given in following Fig. 4-7, are only the evidence values. They are not to be the conditional probabilities. DAG models which are sub models of TBN are given following for illustrate the Scenarios.



**Figure 4.** DAG model of Scenario-A with Evidence values

**Scenario-A:** Index values of XUTUM are examined as Scenarios-A for decreasing, recession, and increasing conditions, respectively. The mathematical model of Scenario-A is given in Eq. (3).

$$\begin{aligned}
 p(XUTUM, XULAS, XKAGT, XHOLD, XBLSM, XILTM, XINSA, XYORT) &= p(XUTUM) \\
 & p(XKAGT | XUTUM) p(XILTM | XULAS) p(XULAS | XUTUM) \\
 & p(XBLSM | XULAS) p(XINSA | XHOLD) p(XHOLD | XUTUM) p(XYORT | XHOLD)
 \end{aligned}
 \tag{3}$$

DAG of Scenario-A is an abbreviated version of BN model given in Fig. 5. Decreasing, recession and increasing probabilities of model are similar for XHOLD, XKAGT, XULAS and XUTUM. XUTUM index directly affect previously mentioned indexes. In the Table 2, XBANK, XHOLD and XUHIZ indexes are made their declining and upward trends in enormous quantities with XUTUM. In addition to this, predicted probabilities of XGMYO are obtained 62.2% for decrease, 2% for recession and 35.8% for increase. The predicted probabilities of the XGOLD are 51.2%, 2.3% and 46.5%, respectively. If XUTUM index known recession, as can be understood from the Table 2, XGOLD index will not be much affected by the XUTUM index probabilities. The estimated probability of returns indexes and foreign exchange rates are not affected by the stock market indexes such as XGOLD. When XUTUM index given recession, posterior probability of the XYLDZ index is 86.1% decreasing. But estimated recession probability is 13.6%. Likewise, posterior probabilities of other stock market indexes are calculated like the first scenario in Table 2. In other words, other financial instruments have not been affected by the prior knowledge of the XUTUM index. Furthermore, the conditional probabilities of the other indexes and the foreign exchange rates are calculated when the XUTUM index is given as evidence of an increasing. The calculated probabilities are similar to the decrease of the XUTUM index.



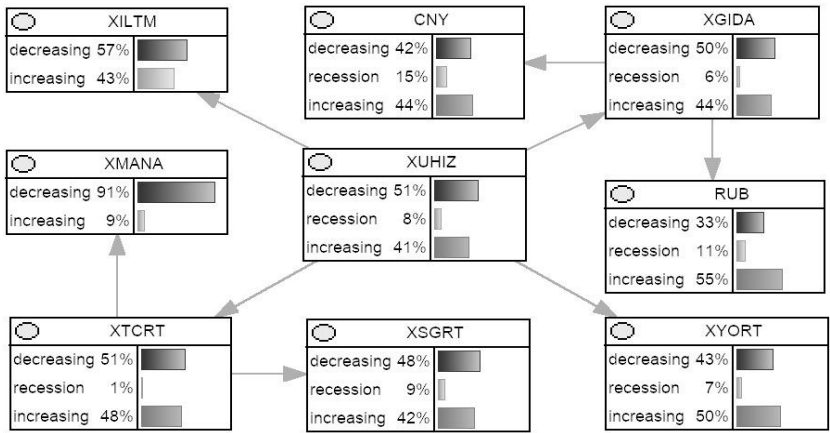


Figure 5. DAG model of Scenario-B with Evidence values

**Scenario-B:** Index values of XUHIZ are examined as Scenarios-B for decreasing, recession and increasing conditions, respectively. The mathematical model of Scenario-B is given in Eq. (4).

$$\begin{aligned}
 & p(XUHIZ, XYORT, XGIDA, XILTM, XMANA, XTCRT, RUB, CNY, XSGRT) = p(XUHIZ) \\
 & p(XYORT / XUHIZ) p(XBLSM / XUHIZ) p(RUB / XGIDA) p(XYORT / XUHIZ) p(CNY / XGIDA) \quad (4) \\
 & p(XMANA / XTCRT) p(XTCRT / XUHIZ) p(XSGRT / XTCRT)
 \end{aligned}$$

In this scenario, while decreasing condition of XUHIZ index is known XUTUM, XU100, XYLDZ, XBANK indexes will be decreased by 70% - 75%. Besides, the probability of XGOLD, XGMYO and XGIDA indexes to take a decreasing value is between 50% and 55%. On the other hand, exchange rates are maintained the general probability values. They have an insignificant amount of relation to XUHIZ. It is shown Table 2 that, when the XUHIZ index is to be recession, other variables are moving in the range of 45% to 55% of the probability that they are not influenced by this situation. Also, increasing probabilities of the XUHIZ indexes are similar to decreasing probabilities.

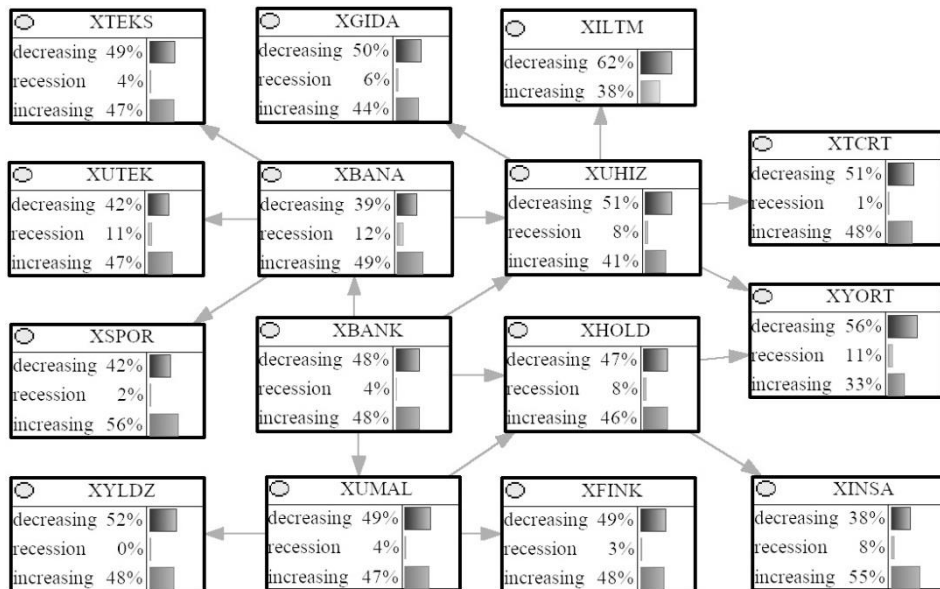


Figure 6. DAG model of Scenario-C with Evidence values

**Scenario-C:** Index values of XBANK are examined as Scenario-C for decreasing, recession and increasing conditions, respectively. The mathematical model of Scenario-C is given in Eq. (5).

$$p \left( \begin{matrix} XBANK, XUHIZ, XBANA, XUMAL, XHOLD, XYORT, XTERT, XILTM, XGIDA, \\ XTEKS, XUTEK, XSPOR, XYLDZ, XFINK, XCONST \end{matrix} \right) = p(XBANK) \tag{5}$$

$$p(XTERT / XUHIZ) p(XUHIZ / XBANA, XBANK) p(XBANA / XBANK) p(XILTM / XUHIZ)$$

$$p(XGIDA / XUHIZ) p(XTEKS / XBANA) p(XUTEK / XBANA) p(XSPOR / XBANA) p(XYLDZ / XUMAL)$$

$$p(XUMAL / XBANK) p(XFINK / XUMAL) p(XINSA / XHOLD) p(XHOLD / XUMAL, XBANK)$$

$$p(XYORT / XHOLD, XUHIZ)$$

In Fig. 7 it is understood that, XBANK have a direct relation with XBANA, XUMAL, XHOLD and XUHIZ indexes and indirect relation with other variables. The Turkish banking sector is important in terms of showing the strength of the Turkish financial market. For this reason, Scenario-C has been formed with the XBANK index. In these scenarios, it is understood that the XBANK index and XUTUM, XU100, XYLDZ and XHOLD indexes generally act jointly. While XUHIZ index is shown a decreasing tendency in decreasing condition of the XBANK index, it is observed to be less affected in other cases. These arguments of XBANK index have negligible effect on the conditional probabilities of other variables.

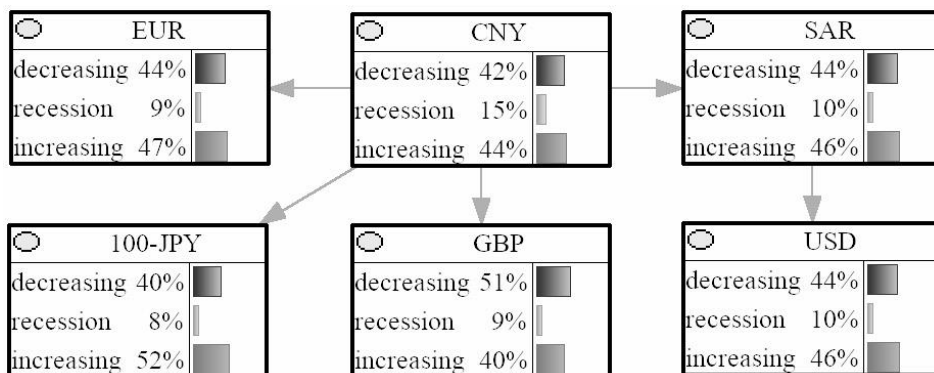


Figure 7. DAG model of Scenario-D with Evidence values

**Scenario-D:** Foreign exchange rate values of CNY examined as Scenario-D for decreasing, recession and increasing conditions, respectively. The mathematical model of Scenario-D is given in Eq. (6).

$$p(CNY, GBP, SAR, 100-JPY, USD, EUR) = p(CNY)p(USD / SAR)p(SAR / CNY) p(EUR / CNY)p(100 = JPY / CNY)p(GBP / CNY) \tag{6}$$

CNY exchange rate has a direct relation with EUR, SAR and GBP. But, USD has an indirect relation with CNY. This information explains the positive trade relations that have developed in recent years with Asia and Africa. In addition, agreements for the use of national exchange rates in foreign trade may be effective in revealing the relationship between foreign exchange variables.

In addition, in Table 2 decreasing is given as prior for USD, EUR and GBP affected negatively. Although those were not affected in the recession prior, there was a tendency to increase in the given ascending prior state. XGIDA has shown a positive trend in the case of USD's recession and a negative trend with negligible impact from USD's increasing prior.

As a result, when the all scenarios are examined, XGOLD and foreign exchanges are not influenced by the tendency of the stock market indexes. It can be said that the characteristics of these three different types of investment instruments are different. Their interactions with each other are minimal. On the other hand, there is a similarity in homogeneous type of instrument data. It is maintained that, index variables have influenced by index variables, foreign exchange variables influenced by other foreign exchange variables. In addition, gold index shows an independent change from other two types of investment tools.

#### 4. CONCLUSION

The model is designed for the day-to-day of 31 BIST return indexes and 7 foreign exchange rates from the beginning of the year to September 30, 2016. Predictions are made on the main model for the period after the coup attempt. The model has been established to monitor the first impact of the attempt on the market and so, does not reflect the profound impact that may arise in the long term.

The model has been set up differently from the normal BN and has been validated with real data set instead of the generated data from the established model. As a result, accuracy rate of the model has been calculated from the real dataset 85.5% percent. Usages of real data ensure that, BN model can be re-trained. Thus, it is possible to calculate the conditional probabilities of variables in different conditions in TBN model.

The results of analysis showed that BNs are an effective method for market research, considering the interaction between BIST returns indexes and foreign exchange rates. The government, using the information in the TBNs and the knowledge of Turkey Financial Market, they can make decisions backed by scientific and objective tool. To summarize, the dynamic nature of BNs not only defines the real situation, it also allows the Turkish economy to simulate any external impact (i.e., coup attempt) in real time.

### Acknowledgment

All Bayesian models were analyzed and graphed using GeNIe Modeler version 2.2 academic edition software developed at BayesFusion, LLC in <http://www.bayesfusion.com>.

Ersin Sener, this author is a scholarship of Technological Research Council of Turkey (TÜBİTAK) 2211-A Domestic Doctoral Scholarship Program.

### Conflict of interest

None of the authors of this paper have a financial or personal relationship with other people or organizations that could inappropriately influence or bias the content of the paper.

### Author biography

**Ersin Sener** is a research assistant at the department of mathematics in Kırklareli University. And he is a PhD candidate at the department of mathematics in Yildiz Technical University. His main research topics are Bayesian statistical analysis, education and statistical research.

**Hasan Aykut Karaboga** is a research assistant at the department of statistics in Yildiz Technical University. And he is a PhD candidate at the same department. He studies on Bayesian statistics, multivariate statistical methods, data mining and artificial intelligence.

**Ibrahim Demir** is an associate professor at the department of statistics in Yildiz Technical University. His research areas are educational statistics, multivariate methods and data mining in social sciences.

### REFERENCES

- [1] Chickering, D. M. (2002): Learning equivalence classes of Bayesian-network structures. *Journal of machine learning research*, 2(Feb): 445-498.
- [2] Neapolitan, R. E. (2004): *Learning Bayesian networks* (Vol. 38). Upper Saddle River, NJ: Pearson Prentice Hall.
- [3] Aghaie, A.- Saeedi, A. (2009, April): Using Bayesian networks for bankruptcy prediction: Empirical evidence from Iranian companies. In *Information Management and Engineering*, 2009. ICIME'09. International Conference on: 450-455. IEEE.
- [4] Sun, L.- Shenoy, P. P. (2007): Using Bayesian networks for bankruptcy prediction: Some methodological issues. *European Journal of Operational Research*, 180(2): 738-753.
- [5] Sarkar, S.- Sriram, R. S. (2001): Bayesian models for early warning of bank failures. *Management Science*, 47(11):1457-1475.
- [6] Leong, C. K. (2016): Credit risk scoring with Bayesian network models. *Computational Economics*, 47(3): 423-446.
- [7] Pavlenko, T.- Chernyak, O. (2010): Credit Risk Modeling Using Bayesian Networks. *International Journal of Intelligent Systems*, 25(4): 326-344.
- [8] Abramowicz, W.- Nowak, M.- Szykiel, J. (2003): Bayesian networks as a decision support tool in credit scoring domain. In P. C. Pendharkar (Ed.), *Managing data mining technologies: Techniques and applications: 1–20*. Hershey: Idea Group Publications.

- [9] Shenoy, C.- Shenoy, P. P. (2000): Bayesian Network Models of Portfolio Risk and Return. The MIT Press.
- [10] De Giuli, M. E.- Maggi, M. A.- Tarantola, C. (2010): Bayesian outlier detection in capital asset pricing model. *Statistical Modelling*, 10(4): 375-390.
- [11] Wijayatunga, P.- Mase, S.- Nakamura, M. (2006): Appraisal of companies with Bayesian networks. *International Journal of Business Intelligence and Data Mining*, 1(3): 329-346.
- [12] Donaldson Soberanis, I. E. (2010): An extended Bayesian network approach for analyzing supply chain disruptions. PhD Thesis, University of Iowa.
- [13] Cattell D.- Love, P.E.D. (2013): Using Bayesian Networks to assess the risk appetite of construction contractors. *38th Australian University Building Educators Association Conference*. Auckland:New Zealand.
- [14] Zuo, Y.- Kita, E. (2012): Stock price forecast using Bayesian network. *Expert Systems with Applications*, 39(8): 6729-6737.
- [15] Baesens, B.- Egmont-Petersen, M.- Castelo, R.- Vanthienen, J. (2002): Learning Bayesian network classifiers for credit scoring using Markov Chain Monte Carlo search. In *Pattern Recognition, 2002. Proceedings. 16th International Conference on*, 3:49-52. IEEE.
- [16] Gemela, J. (2001): Financial analysis using Bayesian networks. *Applied Stochastic Models in Business and Industry*, 17(1): 57-67.
- [17] Gemela, J. (2003): Learning Bayesian networks using various data sources and applications to financial analysis. *Soft Computing*, 7(5): 297-303.
- [18] Wu, Y.- McCall, J.- Corne, D. (2010): Two novels Ant Colony Optimization approaches for Bayesian network structure learning. In *Evolutionary Computation (CEC), 2010 IEEE Congress on*: 1-7. IEEE.
- [19] Zuo, Y.- Kita, E. (2012): Up/down analysis of stock index by using Bayesian network. *Engineering Management Research*, 1(2): 46.
- [20] Takci, B. B. H.- Ekinici, U. C. (2011): Bank credit risk analysis with bayesian network decision tool. *International Journal Of Advanced Engineering Sciences And Technologies*, 9(2): 273-279.
- [21] Weber, P.- Medina-Oliva, G.- Simon, C.- Iung, B. (2012): Overview on Bayesian networks applications for dependability, risk analysis and maintenance areas. *Engineering Applications of Artificial Intelligence*, 25(4): 671-682.
- [22] Olbryś J. (2009): Forecasting Portfolio Return Based on Bayesian Network Model. [in:] W.Milo, G.Szafranski, P.Wdowiński (eds.): *Financial Markets. Principles of Modelling, Forecasting and Decision-Making*, FindEcon Monograph Series: Advances in Financial Market Analysis, Lodz University Press, 7:157-171.
- [23] Chernyak, O., Chernyak, Y. (2011): Classification of Financial Conditions of the Enterprises in Different Industries of Ukrainian Economy Using Bayesian Networks. In *HAICTA*: 519-530.
- [24] Tarantola, C., Vicard, P.- Ntzoufras, I. (2012): Monitoring and improving Greek banking services using Bayesian Networks: An analysis of mystery shopping data. *Expert systems with applications*, 39(11): 10103-10111.
- [25] Shen, C. W. (2009): A bayesian networks approach to modeling financial risks of e-logistics investments. *International journal of information technology & decision making*, 8(04): 711-726.
- [26] Druzdzel, M. J. (1999): GeNIe: A development environment for graphical decision-analytic models. In *Proceedings of the AMIA Symposium*. American Medical Informatics Association :1206.
- [27] Pearl, J. (1988): Probabilistic reasoning in intelligent systems: networks of plausible inference. Morgan Kaufmann, San Mateo: CA.
- [28] Heckerman, D.- Geiger, D.- Chickering, D. M. (1995): Learning Bayesian networks: The combination of knowledge and statistical data. *Machine learning*, 20(3): 197-243.

- [29] Jensen, F. V (1996): An introduction to Bayesian Networks, UCL Press, London.
- [30] Cowell, R. G.- Dawid, A. P.- Lauritzen, S. L.- Spiegelhalter, D. J. (1999): Probabilistic Networks and Expert Systems, Springer: New York.
- [31] Cooper, G.F.- Herskovits, E.A. (1992): A Bayesian method for the induction of probabilistic networks from data, *Machine Learning*, 9: 309-347.
- [32] Pearl, J.- Verma, T. S. (1995): A theory of inferred causation. In *Studies in Logic and the Foundations of Mathematics*, 134: 789-811. Elsevier.
- [33] Kayaalp, M.- Cooper, G. F. (2002, August): A Bayesian network scoring metric that is based on globally uniform parameter priors. In *Proceedings of the Eighteenth conference on Uncertainty in artificial intelligence*, Morgan Kaufmann Publishers Inc. : 251-258.
- [34] Buntine, W. (1991): Theory refinement on Bayesian networks. In *Uncertainty Proceedings 1991*: 52-60.
- [35] Cheng, J.- Bell, D. A.- Liu, W. (1997): An algorithm for Bayesian belief network construction from data. In *proceedings of AI & STAT'97*: 83-90.
- [36] Hesar, A. S.- Tabatabaee, H.- Jalali, M. (2012): Structure learning of bayesian networks using heuristic methods. In *Proc. of International Conference on Information and Knowledge Management*.
- [37] Galapero, J.- Fernández, S.- Pérez, C. J.- Calle-Alonso, F.- Rey, J.- Gómez, L. (2016): Identifying risk factors for ovine respiratory processes by using Bayesian networks. *Small Ruminant Research*, 136: 113-120.
- [38] Dechter, R. (1992): *Constraint networks*. Information and Computer Science, University of California: Irvine.
- [39] Becker, A.- Geiger, D. (1996): Optimization of Pearl's method of conditioning and greedy-like approximation algorithms for the vertex feedback set problem. *Artificial Intelligence*, 83(1): 167-188.
- [40] Onisko, A.- Druzdzel, M. J. (2003, October): Effect of imprecision in probabilities on Bayesian network models: An empirical study. In *Working notes of the European Conference on Artificial Intelligence in Medicine (AIME-03): Qualitative and Model-based Reasoning in Biomedicine*. Protaras: Cyprus (October 18–22 2003).
- [41] Swets, J. A. (2014): Signal detection theory and ROC analysis in psychology and diagnostics: Collected papers. Psychology Press.

**Appendix**

**Appendix A: Codes and Descriptive Statistics**

**Table A.1** Variable Names, Codes and Descriptive Statistics

|    | <b>INDEX CODE</b> | <b>INDEXES</b>             | <b>MEAN</b> | <b>STDANDART DEVIATION</b> |
|----|-------------------|----------------------------|-------------|----------------------------|
| 1  | 100-JPY           | 100 JAPANESE YEN           | 0.114       | 0.988                      |
| 2  | CNY               | CHINESE YUAN               | 0.003       | 0.591                      |
| 3  | EUR               | EURO                       | 0.032       | 0.563                      |
| 4  | GBP               | BRITISH POUND              | -0.051      | 0.776                      |
| 5  | RUB               | RUSSIAN ROUBLE             | 0.101       | 1.125                      |
| 6  | SAR               | SUUDI ARABIA RIAL          | 0.018       | 0.631                      |
| 7  | USD               | UNITED STATES DOLLAR       | 0.018       | 0.631                      |
| 8  | XGOLD             | GOLD INDEX                 | 0.126       | 1.093                      |
| 9  | XBANA             | BIST MAIN                  | 0.062       | 1.598                      |
| 10 | XBANK             | BIST BANKS                 | 0.065       | 1.818                      |
| 11 | XBLSM             | BIST INF. TECHNOLOGY       | 0.058       | 1.397                      |
| 12 | XELKT             | BIST ELECTRICITY           | 0.026       | 1.609                      |
| 13 | XFINK             | BIST LEASING FACTORING     | 0.170       | 1.301                      |
| 14 | XGIDA             | BIST FOOD BEVERAGE         | 0.027       | 1.622                      |
| 15 | XGMYO             | BIST REAL EST. INV. TRUSTS | 0.072       | 1.508                      |
| 16 | XHOLD             | BIST HOLD. AND INVESTMENT  | 0.058       | 1.504                      |
| 17 | XILTM             | BIST TELECOMMUNICATION     | 0.008       | 1.493                      |
| 18 | XINSA             | BIST CONSTRUCTION          | 0.034       | 1.717                      |
| 19 | XKAGT             | BIST WOOD PAPER PRINTING   | 0.003       | 1.333                      |
| 20 | XKMYA             | BIST CHEM. PETROL PLASTIC  | -0.018      | 1.346                      |
| 21 | XMADN             | BIST MINING                | 0.198       | 3.720                      |
| 22 | XMANA             | BIST BASIC METAL           | 0.158       | 1.903                      |
| 23 | XMESY             | BIST METAL PRODUCTS MACH.  | 0.098       | 1.511                      |
| 24 | XSGRT             | BIST INSURANCE             | 0.017       | 0.778                      |
| 25 | XSPOR             | BIST SPORTS                | 0.295       | 2.892                      |
| 26 | XTAST             | BIST NONMETAL MIN. PRODUCT | 0.044       | 1.218                      |
| 27 | XTCRT             | BIST W. AND RETAIL TRADE   | -0.005      | 1.504                      |
| 28 | XTEKS             | BIST TEXTILE LEATHER       | 0.123       | 1.560                      |
| 29 | XTRZM             | BIST TOURISM               | -0.018      | 1.940                      |
| 30 | XU100             | BIST 100                   | 0.045       | 1.409                      |
| 31 | XUHIZ             | BIST SERVICES              | -0.024      | 1.221                      |
| 32 | XULAS             | BIST TRANSPORTATION        | -0.172      | 1.875                      |
| 33 | XUMAL             | BIST FINANCIALS            | 0.041       | 1.183                      |
| 34 | XUSIN             | BIST INDUSTRIALS           | 0.052       | 1.262                      |
| 35 | XUTEK             | BIST TECHNOLOGY            | 0.047       | 1.573                      |
| 36 | XUTUM             | BIST ALL SHARES            | 0.042       | 1.356                      |
| 37 | XYLDZ             | BIST STARS                 | 0.040       | 1.372                      |
| 38 | XYORT             | BIST INVESTMENT TRUSTS     | -0.005      | 1.018                      |